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#### **Phase-Field Modeling of Technical Important Alloys**

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#### Outline

- 1. Introduction
- 2. Pragmatic Multi-Phase-Field Model
- 3. Coupling to Thermodynamic Data: Quasi-Equilibrium
- 4. Simulation of Technical Alloys and Processes: Examples

  a) Linking to the Process: The General Micro-Macro Problem
  b) "Bridgman" Approximation: Directional Solidification
  c) "DTA" Approximation: Small Samples
  d) Homoenthalpic Approximation: External 1D-Temperature Field
- 5. Conclusion





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#### Introduction: Phase-Field Simulation of Complex Technical Microstructures

#### Challenges linked with simulation of technical microstructures:

- complex alloys
  - complex morphologies
    - complex thermodynamics
      - complex processes





#### What is a 'pragmatic' phase-field approach?

- multiphase-field model which allows simulation on µm scale
- online-coupling to off-the-shelf thermodynamic and diffusion databases
- advanced thermal coupling to external process conditions
- pragmatic simulation strategy (calibration, simplifications)
- robust multi-purpose code (no dedicated solutions)







#### **MICRESS: MICRostructure Evolution Simulation Software**

Can be applied to composition, temperature or curvature controlled transformations on the microscale:

- Solidification (dendritic, cellular, peritectic, eutectic)
- Solid state reactions (grain growth, recrystallisation, phase transformations)
- Direct coupling to thermodynamic databases (contains TQ-interface\*) or linear phase diagram approximation







multiphase multicomponent

\*from Thermo-Calc Software, Sweden





#### The MICRESS® Story



**1995: first microstructure simulations at ACCESS** 

1996: multi-phase-field model published (Physica D 94(1996), p.135-147.)

**1999: simulations comprising thermodynamic databases** 

2003: MICRESS is commercially available

2005: MICRESS website is online: www.micress.de

2006: stress solver incorporated

2007: coupling to external temperature fields

2008: MICRESS user forum on website: www.micress.de/forum

2009: incorporation of nple and para-equilibrium models

2010: higher order terms for triple junctions etc.

2011: Version 6.0: 64bit Version with TQ





#### We.....the MICRESS group at Access:



Dr. Markus Apel Dr. Bernd Böttger **Dr. Antoine Carre** Dr. Janin Eiken (formerly: J. Tiaden) Dr. Georg J. Schmitz **Alexandre Viardin** Kathrin Graetz (master student) New member: Ralph Altenfeld





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#### **Phase-Field Model**

Diffuse interface, described by the phase-field parameter  $\phi$ :



- The order parameter  $\phi = \phi(x,t)$  corresponds to a density function for the phase state.
- $\eta$  is the interface thickness (numerical parameter)





#### **The Multiphase-Field Model**

$$\{\phi_{\alpha}\} \alpha = 1...N$$

$$f = \sum_{\alpha \neq \beta} f_{\alpha\beta} \left(\{\phi_{\alpha}\}\right) + f_{c}$$

$$= \sum_{\alpha,\beta} \frac{\sigma_{\alpha\beta}(\vec{n}_{\alpha},\vec{n}_{\beta})}{\eta_{\alpha\beta}} K^{\alpha\beta} (\Delta\phi_{\alpha},\Delta\phi_{\beta},\phi_{\alpha},\phi_{\beta}) + \sum_{\alpha} \phi_{\alpha} f^{\alpha} (c_{\alpha})$$

$$\Psi_{\alpha\beta} = \left(\frac{\delta}{\delta\phi_{\alpha}} - \frac{\delta}{\delta\phi_{\beta}}\right) f \qquad \dot{\phi}_{\alpha} = \sum_{\beta} \mu_{\alpha\beta} \Psi_{\alpha\beta}$$

Vector order parameter

 $f_{\alpha\beta}$ : pair interaction energies  $f_c$ : chemical free energy

 $\psi_{\alpha\beta}~$  : interfacial growth operator

#### what is pragmatic?

- bulk thermodynamic data are used only for the chemical free energy  $f_c$
- **I**  $f^{\alpha}$  is a function of  $c_{\alpha}$ , not of c!
- $\rightarrow$  coupling to arbitrary thermodynamic databases possible!





#### **Multiphase-field equation:**



- $\eta_{\alpha\beta}$  = interface thickness
- $\mu_{\alpha\beta}$  = interfacial mobility (anisotropic)
- $\sigma_{\alpha\beta}$  = interfacial energy (anisotropic)
- $\Delta G_{\alpha\beta}$  =  $\mbox{ driving force}$

Steinbach et al; Physica D 1996
Tiaden et al. Physica D 1998
Steinbach, Pezzolla; Physica D 1999
Eiken, Böttger, Steinbach; Phys. Rev. E 2006





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#### Phase-Field and Thermodynamics: Quasi-Equilibrium

• minimization of the chemical free energy  $f_c = \sum \phi_{\alpha} f_{\alpha}$  at constant phase fractions  $\phi_{\alpha}$  gives: β α  $\Delta G_{\alpha}$ Φβ  $\phi_{\alpha}$ •  $\Delta G_{\alpha\beta}$ ,  $C_{\alpha}^{k}$  and  $C_{\beta}^{k}$  are calculated iteratively including the mass balance:  $\phi_{\alpha} c_{\alpha}^{k} + \phi_{\beta} c_{\beta}^{k} = c^{k}$ 





#### Phase-Field and Thermodynamics: Multiphase Quasi-Equilibrium

additional phases are included into the iteration process:



iteration for N phases:

$$\Delta G_{\alpha\beta} = f_{\alpha} - f_{\beta} + \sum_{k} \tilde{\mu}^{k} \left( c_{\alpha}^{k} - c_{\beta}^{k} \right) \quad , \quad \tilde{\mu}^{k} = \frac{df_{\alpha}}{dc_{\alpha}^{k}} = \frac{df_{\beta}}{dc_{\beta}^{k}} = \frac{df_{\gamma}}{dc_{\gamma}^{k}} \dots,$$

 $\sum_{i} \phi_i c_i^k = c^k$ 

- consistent quasi-equilibria for all phase pairs
- problem: huge calculation times!



#### **Phase-Field and Thermodynamics: Multi-Binary Extrapolation**



#### Use of Thermodynamic Data in MICRESS®



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#### Linking to the Process: The General Micro-Macro Problem



General micro-macro problem:

- Microstructure simulation needs temperature information from the macro-scale
- Macroscopic simulation needs latent heat effects from the micro-scale

→ Exact solution would require microstructure simulation on the **whole** casting!

 $\rightarrow$  Which approximations are reasonable?





#### Typical approximations for phase-field simulation:

- no latent heat is taken into account
  - e.g. ripening, grain growth
  - slow processes (e.g. solid-solid)
  - high temperature gradient (Bridgman process)
- global temperature effect (G=0)
  - slow processes in thermally isolated materials
  - small samples (DTA)
- temperature is solved on different scale (e.g. free growing dendrite)
  - special assumptions are needed





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#### "Bridgman" Approximation

#### Bridgman Apparatus:

-large constant thermal gradient -pulling velocity is controlled

→ T gradient and cooling rate practically are independent!

#### "Bridgman" Approximation:

- T gradient and cooling rate are regarded as independent external parameters for microstructure simulation
- are taken from experiments or process simulation results

#### Problem with Approximation:

- thermal conditions may be not consistent with microstructure formation
- $\rightarrow$  "violation" of microstructure







#### **2D Representations of Directional Dendritic Growth**

G

 3D simulations are possible with MICRESS<sup>®</sup>, but need a high computational effort. At present, 3D is not realistic for:

> multicomponent technical alloy simulation of complete solidification (evtl. with precipitation of secondary phases)

⇒ Simulation of reasonable 2D projections!



hexagonal symmetry of the crystal lattice





#### 2D Representations of Directional Dendritic Growth: Longitudinal Projection

#### a) longitudinal projection

define T-gradient in z-direction and cooling rate

```
# Initial temperature at the bottom? (real) [K]
1660.000
# Temperature gradient in z-direction? [K/cm]
50.0000
# Cooling rate? [K/s]
-2.5000
```

## smallest unit cell is $\frac{1}{2}$ dendrite with symmetric boundary conditions

```
# Boundary conditions for phase field in each direction
# Options: i (insulation) s (symmetric) p (periodic/wrap-around)
# g (gradient) f (fixed) w (wetting)
# Sequence: E W (N S, if 3D) B T borders
ssii
#
# Boundary conditions for concentration field in each direction
# Options: i (insulation) s (symmetric) p (periodic/wrap-around) g
(gradient) f (fixed)
# Sequence: E W (N S, if 3D) B T borders
ssii
```

#### initial seed at lower left corner









## Example 1:

### Solidification of Stainless Steel





#### **Solidification of Stainless Steel**







#### **Solidification of Stainless Steel**





## Example 2:

### Solidification and Heat Treatment of a Technical Ni-Base Superalloy

### (removed for confidentiality)







## Example 3:

### **Directional Solidification of CMSX-4**





#### Average composition for simulation:

element	Cr	Со	Мо	W	Ta	AI	Ti	Re	Hf
wt %	6,5	9	0,6	6	6,5	5,6	1	3	0,1

#### Casting of cylindrical geometry using a Bridgman furnace

TTNI7

v [mm/min]	8,6
G [K/mm]	4,5
λ [µm]	199

Thermodynamic database:

Mobility database:

**MOBNI** for diffusion in fcc (incl. cross terms)





#### **Directional Solidification of CMSX-4**









## Example 4:

### Remelting of IN706 – Moving Frame





2D Simulation with "moving frame":

	Ni	Fe	Cr	Ti	Nb	A	С
at%	bal	37.7	17.1	1.83	1.8	0.55	0.05



0.024

0.022

0.020

0.018

0.016

0.014

0.012

0.010

8·10<sup>-5</sup>

#### b) transversal isothermal projection

define cooling rate without T-gradient

```
# Initial temperature at the bottom? (real) [K]
1660.000
# Temperature gradient in z-direction? [K/cm]
0.0000
# Cooling rate? [K/s]
-2.5000
```

## smallest unit cell is ${}^1\!\!\!/_4$ dendrite with symmetric boundary conditions

quadratic domain with initial seed at lower left corner









## Example 5:

### ESU Solidification of IN718

(removed for confidentiality)





#### **ESU Solidification of IN718: Array with Grain Boundary**

- simulation domain: 500 x 500  $\mu m$
- grid resolution: 2  $\mu m$
- 2 grains with regular array of different orientations

- $\rightarrow$  more realistic
- $\rightarrow$ improved statistics on phase fractions etc.









## Example 6:

### CMSX-4: continued





#### CMSX-4: continued







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#### **"DTA"** Approximation



- no problems with consistency of temperature with microstructure, but
- $\rightarrow$  huge unrealistic recalescence





## Example 7:

### Grain Size of Magnesium Alloys AZ31, AZ61, AZ91





#### density 1.8e+07 1.6e+0 1.4e+07 nucleant distribution nucleant positioning 1.2e+07 1e+07 8e+06 6e+06 4e+06 **Nucleation-Model** 2e+06 0 0.2 0.4 0.6 0.8 $|\Delta T_{crit}(r)| < \Delta T(\bar{c},T)$ ? radius critical undercoolimg nucleants with new nucleus different radii Multi-Phase-Field-Solver **Multicomponent Diffusion-Solver** 2 r $\Delta T_{crit}(r) = \frac{2\sigma}{\Delta S \cdot r}$ **Temperature-Solver** MICRESS® nuclei

#### Grain Size of Magnesium Alloys AZ31, AZ61, AZ91: Nucleation Modell

#### Grain Size of Magnesium Alloys AZ31, AZ61, AZ91



increased	a	luminium	content
moreacea	~		••••••

AZ31

decreased grain size





**AZ91** 



#### Grain Size of Magnesium Alloys AZ31, AZ61, AZ91: Nucleation Modell

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#### **Multiphase-Field Model with Integrated 1D Temperature Solver**







#### Linking to the Process: A Virtual Solidification Experiment for AI-3at%Cu Plate Casting



#### Linking to the Process: Homoenthalpic Approach



- converging rapidly, leading to a self-consistent solution
- differences are small, but in critical temperature range
- Strong effect on grain size!







#### Linking to the Process: Homoenthalpic Approach





- after iteration H(T) is very similar for different positions in the virtual casting!
- Homoenthalpic approximation (assumption of a global H(T) relation) is reasonable in this case!

# Homoenthalpic Approach allows for an iterative solution of the general micro-macro problem!







## Example 8:

### Equiaxed Solidification of IN738







Position 1

Position 2









#### Equiaxed Solidification of IN738







#### Equiaxed Solidification of IN738: Different Cooling Conditions









IN738 + 2% Nb



## Example 9:

### Piston Alloy KS1295





#### **Piston Alloy KS1295: Simulation Setup**



- include elements Al Si Cu Mg Ni Fe Mn Zn
- include all phases which may appear during solidification
- unit cell model for ¼ grain
- FD grid with 400 x 400 cells and 0.5 µm resolution
- realistic temperature field from external 1D simulation using the Homoenthalpic Approximation



- coupling to thermodynamic database TTAL5
- coupling to diffusion database MOBAL1





#### **Piston Alloy KS1295: Segregation and Intermetallic Phases**



#### **Piston Alloy KS1295: Simulation Details**



#### Phase Identification using EDX and EBSD (piston alloy similar to KS1295)





C-L Chen and R.C.Thomson, 12th Conference on EBSD at the University of Manchester, April 2005







#### Example1: Alloy KS1295 (AI-Si-Fe-Ni-Cu-Mg-Zn), Comparison to Quantitative Metallography



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- For PF microstructure simulation in complex technical applications a "pragmatic" phase-field approach has to be used
- One needs a proper multiphase-field model which can be applied at various length scales
- Coupling to thermodynamic databases and mobility data is essential for simulation of multicomponent alloys
- Pragmatic approximations have to be found to appropriately couple the PF model to the process conditions
- MICRESS<sup>®</sup> is a commercial software package developed in our research group at ACCESS/Germany which can be applied for research, education and industrial applications







# Thank you for

# your attention!



